

# Forces in Equilibrium + Motion Along an Incline

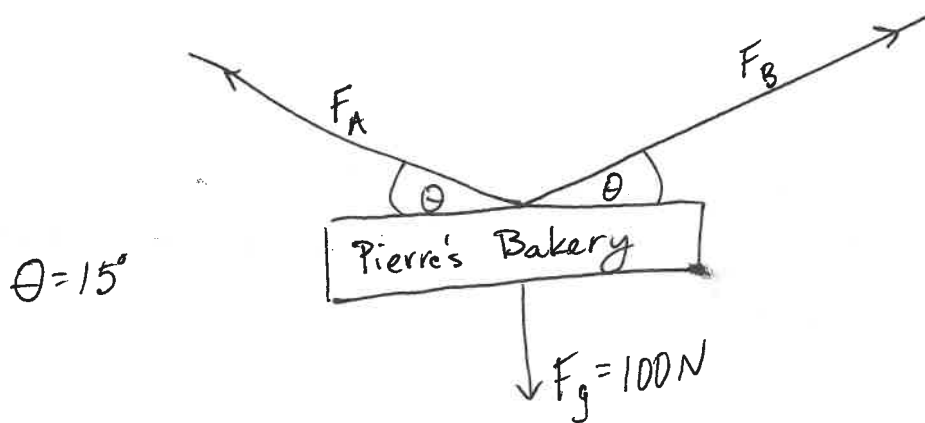
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Equilibrium



Ex. 1

A 100 N sign is hung by two wires as seen below. What is the tension in the wires?



## Performing Calculations for Equilibrium Problems

- Draw a Free-Body Diagram
- List your givens
- List your unknowns
- Isolate your X (horizontal) and Y (vertical) components
- Since the object is in equilibrium,  $F_{\text{net}} = ma = 0$  in both the X and Y directions

### Motion on an Incline:

- When objects are not on a flat, level surface:

•  
•

- Hint:

### Ex. 2

Determine the rate of acceleration of a 25 kg wooden crate as it slides down a wooden ramp with a coefficient of friction,  $\mu = 0.2$ . The angle the ramp makes with the horizontal is  $30^\circ$ .

# Forces in Equilibrium + Motion Along an Incline

## Equilibrium

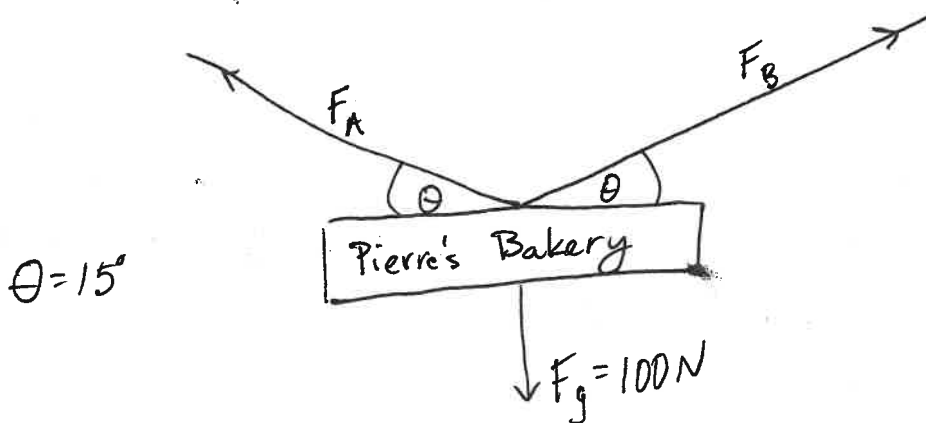
↳ Forces on an object are balanced

↳ Not accelerating

↳ Stationary or moving at a constant speed in a straight line

## Ex. 1

A 100 N sign is hung by two wires as seen below. What is the tension in the wires?



Given:  $F_g = 100\text{ N}$ ,  $\theta = 15^\circ$

Unknown:  $F_A$ ,  $F_B$

X-direction:

$$-F_{Ax} + F_{Bx} = 0$$
$$-F_A \cos \theta + F_B \cos \theta = 0$$
$$F_A \cos \theta = F_B \cos \theta$$

Y-direction:

$$F_{Ay} + F_{By} - F_g = 0$$
$$F_A \sin \theta + F_B \sin \theta - F_g = 0$$
$$2F_A \sin \theta = F_g$$

$$F_A = \frac{F_g}{2 \sin \theta} = \frac{100\text{ N}}{2 \sin(15)} = \frac{100\text{ N}}{0.518}$$

$$F_A = 193\text{ N}$$

$$F_B = 193\text{ N}$$

# Performing Calculations for Equilibrium Problems

- Draw a Free-Body Diagram
- List your givens
- List your unknowns
- Isolate your X (horizontal) and Y (vertical) components
- Since the object is in equilibrium,  $F_{net} = ma = 0$  in both the X and Y directions

## Motion on an Incline:

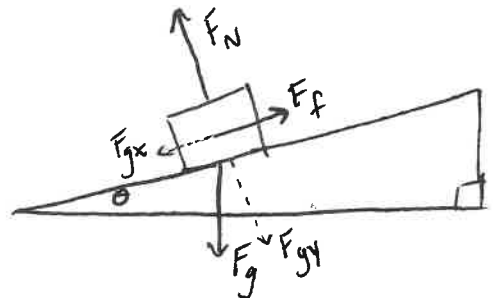
- When objects are not on a flat, level surface:
  - Some of the gravitational force is directed along the surface
  - The Normal Force is not equal to the object's weight
- Hint: Change your coordinate system so the x-axis is parallel to the slope

## Ex. 2

Determine the rate of acceleration of a 25 kg wooden crate as it slides down a wooden ramp with a coefficient of friction,  $\mu = 0.2$ . The angle the ramp makes with the horizontal is  $30^\circ$ .

Given:  $m = 25 \text{ kg}$   
 $\mu = 0.2$   
 $\theta = 30^\circ$   
 $v_i = 0 \text{ m/s}$

Unknown:  $a = ?$



X-direction:

$$F_{net} = F_{gx} - F_f$$
$$ma = m(9.8 \text{ m/s}^2) \sin \theta - \mu F_N$$
$$ma = m(9.8 \text{ m/s}^2) \sin \theta - \mu m(9.8 \text{ m/s}^2) \cos \theta$$
$$a = (9.8 \text{ m/s}^2) \sin \theta - \mu (9.8 \text{ m/s}^2) \cos \theta$$
$$a = (9.8 \text{ m/s}^2) \sin(30^\circ) - (0.2)(9.8 \text{ m/s}^2) \cos(30^\circ)$$
$$a = 3.2 \text{ m/s}^2$$

Y-direction:

$$F_{net} = F_N - F_{gy}$$
$$0 = F_N - F_{gy}$$
$$F_N = F_{gy}$$
$$F_N = m(9.8 \text{ m/s}^2) \cos \theta$$